THE PREDICTION OF RUNNING SPEEDS ON URBAN ARTERIAL STREETS

NOVEMBER 1971 - NUMBER 20



				3047			
							133
				_ (
		77				- 541"	
			- 1				
					0.50		
							4
				,			
					•		
			•			5	
						1	
		4	441			9.5	
,							
							3
						11.5	
							100
						4-25	
	V 10 10 10 10 10 10 10 10 10 10 10 10 10						
				1			
-			100		- E		
		- 10-			E and the		
* 4.5							
the state of							

THE PREDICTION OF RUNNING SPEEDS ON URBAN ARTERIAL STREETS

NOVEMBER 1971 - NUMBER 20

BY

K. A. SHACKMAN

Digitized by the Internet Archive in 2011 with funding from LYRASIS members and Sloan Foundation; Indiana Department of Transportation
http://www.archive.org/details/predictionofrunn00shac

Final Report

THE PREDICTION OF RUNNING SPEEDS ON URBAN ARTERIAL STREETS

TO: J. F. McLaughlin, Director November 23, 1971

Joint Highway Research Project

Project: C-36-17II

FROM: H. L. Michael, Associate Director

Joint Highway Research Project File: 8-4-35

The attached Final Report titled "The Prediction of Running Speeds on Urban Arterial Streets" has been authored by Kenneth A. Shackman, Graduate Assistant in Research on our staff. The research has been supervised by Professor H. L. Michael.

The research reported herein concerns the development of a prediction model for running speeds on urban arterial streets outside of the Central Business District. The determination of the major causes of stop delay and their average values (in time) are also included.

The report is presented as fulfillment of the objectives of the Plan of Study titled as this Final Report and approved by the Advisory Board on September 15, 1970. It is presented for the record and for acceptance.

Respectfully submitted,

Harold L. Michael

Houself 1 Mechant

Associate Director

HLM:ms

cc:	W.	L.	Dolch	R.	н.	Harrell	W.	T.	Spencer
	W.	Η.	Goetz	Μ.	L.	Hayes	J.	Α.	Spooner
	W.	L.	Grecco	R.	D.	Miles	n.	W.	Steinkamp
	Μ.	J.	Gutzwiller	J.	W.	Miller	н.	R.	J. Walsh
	G.	Κ.	Hallock	C.	F.	Scholer	Κ.	B.	Woods
	Μ.	E.	Harr	Μ.	В.	Scott	E.	J.	Yoder



Final Report

THE PREDICTION OF RUNNING SPEEDS ON URBAN ARTERIAL STREETS

by

Kenneth A. Shackman Graduate Assistant in Research

Joint Highway Research Project

Project: C-36-17II

File: 8-4-35

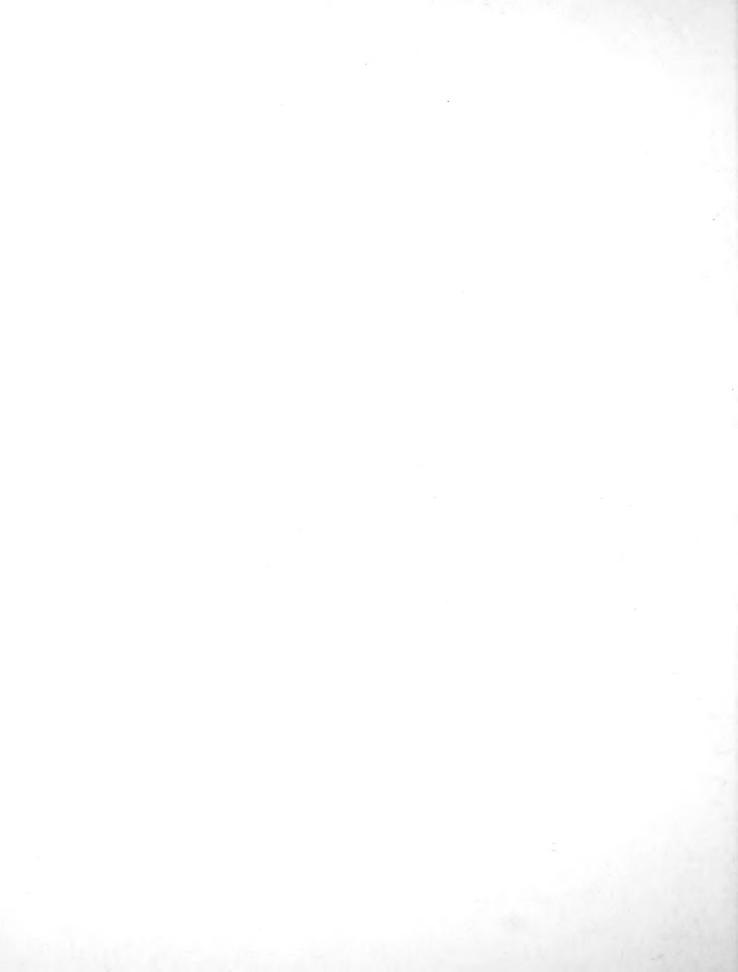
Conducted By

Joint Highway Research Project Engineering Experiment Station Purdue University

In Cooperation With

Indiana State Highway Commission

Purdue University Lafayette, Indiana November 23, 1971



ACKNOWLEDGMENTS

The author wishes to express his gratitude to the Directors of the Joint Highway Research Project for having enabled him to continue his education.

To Mr. Edward J. Kannel for his help, when nothing seemed to be going as planned, and for his moral support and confidence the remainder of the time, the author is indebted.

The esteem of the author goes to Professor H. L. Michael, Head of Transportation and Urban Engineering, School of Civil Engineering, for his guidance in the selection of this topic, for his constructive comments throughout the study, and for his critical review of the manuscript; to Professor V. L. Anderson, Department of Mathematics and Statistics for his advice and review of the statistical analyses and review of the manuscript; and to Professor K. W. Heathington for his advice and review of the manuscript.

Acknowledgment is also given to Mr. George Stafford for his help during the data collection phase of the project.

Thanks go to the many Traffic Engineers, City Engineers, Chiefs of Police, and Police Traffic Officers who assisted in the data collection.

in the data with

TABLE OF CONTENTS

																						Page
LIST	OF T	ABLE	es .	•	•		•	•	•		•	•	•	•	•						•	vi
LIST	OF F	IGUF	RES.		•	•		•	•	•	•	•	•			•	•		•		•	vii
ABST	RACT			•	•			•	•	•	•	•	•		•	•			•	•	•	viii
INTRO	DUCT	ION		•		•	•	•		•	•	•	•			•	•	•	•	•	•	1
	Past	Res	sear	ch	in	ı ı	hi	.s	Ar	ea	١.	•	•	•	•	•	•	•	•	•	•	2
PURPO	OSE.			•	•	•	•	•	•	•	•		•	•	•	•	•	•	•	•	•	5
DATA	COLL	ECTI	ON.	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	7
	Dete Meas	uren	nent	s.	•	•	•	•		•		•	•		Spe	eed.	1	•	•			7
	Sele Data	ctic Col	n c llec	of S ctic	Stu on	ldy Pr	7 5	ec	et i lur	ces	s.	•	•	•	•	•	:	•	•	:	•	9 21
DATA	ANAL	YSIS	s	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•		28
ANAL!	Orig Prel Step The	imir wise Pha Pha Pha Pha Pha Pha	nary e Re ese ese ese ese ese ese ese ese ese	Tegre 1. 2a 2b 3a 4a	est ess	ir	ng on	•	•	•	•	•	•	•	•	•	•	•	•	•	•	28 32 34 35 35 37 37 37
							•					•			-	·						63
	LUSIC		•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	
BIBL	IOGRA NDICE		•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	69
	Appe Q-Te		к A:	. 1	Dis	•	•	sio	on •	oi •	: t	the	e J	Fo:	ste •	er-	-Bı	ur:	c •		•	71



TABLE OF CONTENTS (Continued)

								Page
Appendix	в:	Normality	Test	for	Section	Speeds		75
Appendix	C:	Normality	Test	for	Residual	ls	•	78

41	

LIST OF TABLES

Table			Page
1	Population Groupings of Cities in U.S.A. and Indiana		10
2	Study Cities and Their Classification		12
3	Selected Test Sections With Pertinent Data	•	16
4	Variables Tested in Development of the Model.	•	29
5	Summary of Homogeneity Test Results		33
6	Stepwise Regression Summary Table	•	3 9
7	Results of Testing the Model		44
8	Average Delay Time Per Section (Secs)		50
9	Average Delay Time Per Section (Secs)	•	55
10	Average Delays Due to Traffic Signals, Railroad Crossings, and Other Factors (Secs).	•	59
11	Summary of Speed Influencing Factors	•	67
Append: Table	ix		
ві	Normality Test for Section Speeds (Off-Peak and Peak)		76
cl	Normality Test for Residuals		79

		(4)

LIST OF FIGURES

Figure	Page
1 Frequency of Section Length	. 14
2 Inventory Questionnaire	. 22
3 Data Sheet for Travel Time Study	. 24
4 Summary Sheet for Travel Time Study	. 25
5 Model Inputs	. 36
Appendix Figure	
Bl Frequency of Section Speeds	. 75
Cl Frequency of Residuals	. 78

-

ABSTRACT

Shackman, Kenneth Alan. M.S.C.E., Purdue University, January, 1972. The Prediction of Running Speeds on Urban Arterial Streets. Major Professor: Harold L. Michael.

The purpose of this research project was the development of a model for predicting running speeds on urban arterial streets. To supplement the model the major causes of stop delay and their average values were also evaluated. Using these results one can estimate the change in average running speed and stop delay time between an existing facility and a proposed or improved facility. The estimate of the benefits gained, in terms of time, speed, or money, could then be contrasted with the proposed cost.

The data collection was conducted in nine Indiana cities having populations between thirty and one hundred and fifty thousand; the average car method was the procedure employed for collecting the speed-delay data. Pneumatic tube traffic counters were installed to determine the volumes using the streets being studied.

The prediction model was formulated using stepwise regression. It utilizes eleven roadway and traffic condition variables combined to form ten terms; it has an \mathbb{R}^2 of 0.5926 and a standard error of estimate of 3.417.

The major influences of speed are:

- 1. The length of the section
- 2. The width of the approach
- 3. The number of signalized intersections
- 4. The number of unsignalized intersections
- 5. The number of alleys
- 6. The population of the city
- 7. The number of railroad crossings
- 8. Whether or not parking was allowed on the driver's right
- 9. The volume
- 10. The lowest G/C ratio of the traffic signals included in the section
- 11. Whether or not good progression of the traffic signals existed

The average values of stop delay were calculated from data collected in the speed-delay studies conducted in nine cities. Traffic signals were found to be the major source of stop delays, contributing over eighty percent of the total.

INTRODUCTION

In a recent publication (5) it was stated "that at least as many drivers selected the least 'effort' routes as the least time routes to a shopping center." Just what makes least "effort" routes so inviting? Basically, three elements of high quality of service are considered:

1) safety, 2) constant (or gradually changing) direction, and 3) a constant, reasonable speed. This particular study was concerned with the latter element, speed.

Though a constant speed is desirable the probability of it occurring on an urban arterial street is low, the presence of traffic control devices and a high volume of traffic preventing it. This is true even on streets equipped with progressive signal systems. With proper traffic engineering controls and an adequate design, however, a reasonable average running speed for this type of facility can be obtained.

Average running speed data are widely utilized to determine benefits gained by improvement of the quality of traffic service. This has been accomplished by performing speed-delay studies both before and after implementation of improvements and contrasting the running speeds.

Examples of areas where this has been done include measuring



"the overall effectiveness of traffic control devices", in general (10), and traffic signal timing revisions, in particular, and modifications concerning parking prohibitions, development of one-way street networks, etc. In presenting such accrued benefits of savings in time (or its monetary value) and a usual concurrent reduction of accidents, the engineer has shown the taxpayer, as well as the politician, the value of traffic engineering improvements.

The goal of this study has been to determine a means of predicting the average speed on sections of urban arterials without performing speed-delay studies. This was accomplished by developing a model for predicting the average running speed, employing experimentation and analysis similar to Hejal (7). By estimating average speeds, the time and manpower requirements are reduced, as well as the cost. Indirectly, the major causes of speed reduction and their relative influence have also been determined.

Past Research In This Area

During the past decade there has been some research in the travel time or speed and delay areas. Basically, three different approaches have been tried. They are:

- 1. Computer Simulation
- 2. Before and After Studies
- 3. Models Theoretical and Empirical

	,

Computer simulation appears to be promising; however, this approach has not been perfected to the stage where the results are both workable and representative of reality. There are computer solutions for parts of the problem, such as predicting speeds of vehicles passing through signalized intersections (1) and determining delaying effects of curb parking maneuvers on traffic (19). Though these are steps in the needed direction, the latter, as well as others, did not produce results representative of reality. probable that the development of a realistic simulation program that will encompass all aspects of traffic friction is not in the immediate future. The development of an empirical procedure, however, appears to be a quickly attainable goal since the formulation period would be short and the results might be easily applicable and reasonably accurate.

Edwards and Kelcey (3) reviewed the many parameters of frictional effects on travel time. There were many variables involved in their work in downtown areas. The procedure that was followed was to do "before and after studies" for determining the quantitative effect of individual improvements. These were statistically tested for significance and a Network Assignment Model was applied to determine the overall efficiency of the network. The method worked quite effectively, but it has the disadvantage

		· ·

of being very expensive. Such a method, however, used outside the Central Business District (CBD) where fewer variables would have to be measured and analyzed might be economically reasonable.

Another researcher (5) included change of speed in route evaluation by correlating "cost, comfort, and safety" with a number. The number, however, also was based on change of direction and change of time.

 $N_{t} = \Delta \text{ time } x \Delta \text{ speed } x \Delta \text{ direction}$

The resulting number does not mean anything by itself; it must be compared with another to show relative improvement along a particular section. Unfortunately, this method lumps all the influential factors of quality of service together. The analyzer has no way of determining the cause of quality deterioration, whether it is due to traffic volume or the facility's design characteristics.

Finally, in Hejal's report (7) a regression analysis was used to obtain a relationship between six traffic parameters and the running speed for a two-lane rural highway. Data were collected using the average car method, noting the causes of interference and including other factors or variables from a road inventory. The results obtained compared well with reality and at the same time had a high coefficient of multiple determination (R²). The method proved to be both economical and simple to perform.

			i

PURPOSE

The specific purpose of this research was to develop a model for predicting the average running speeds of vehicles on arterial streets in fringe areas of the CBD.

This, it was assumed, could be achieved by investigating the influence of traffic volume, traffic controls, and design features of the street. This model has two functions: one, to predict the speed that an average vehicle will travel along a facility; and two, to evaluate selected causes of speed reduction.

It is hoped that the proposed model will be useful on all arterial streets, both existing and proposed. On existing streets it should emphasize to the engineer where improvements should be made and their relative benefit. On proposed streets it should indicate during the design stage the average running speed of the vehicles that will use it under anticipated conditions and, if this speed proves to be too low, where design changes need to be made. Another possible use will be the determination of appropriate speed limits.

The engineer today can estimate a desired quality of service from an evaluation of the capacity of a facility. The results of this research will be another tool,

		3	
		,	
(g			

hopefully one which is easier and more accurate of application. The following statement taken from the "Highway Capacity Manual-1965" (9) is a warrant for conduct of this study: "Insufficient data are available to attempt to develop correction factors (on capacity and speed) for such mid-block influences as curb parking." It was apparent that more research was needed on factors affecting average speed.



DATA COLLECTION

Determination of Sample Size for Speed Measurements

At the outset of the data collection stage of the study a section sample size had to be chosen. This sample would consist of a number of running speed observations along one section of roadway in one direction. The decision was made to calculate the size using a statistical approach (more observations would be an inefficient use of both time and money).

Before the calculation of the sample size could be completed certain assumptions had to be made. First, it was assumed that the running speeds recorded on the test sections would be normally distributed. If this were so then the following formula could be used for the calculation:

$$n = z_{\frac{\alpha}{2}}^2 \sigma^2 / E^2. \qquad (14)$$

where

n = sample size

z = table value based on the chosen confidence level

 σ = standard deviation of the population

E = acceptable error

The value of α , the probability of a Type I error chosen was 0.05 and the value of E chosen was \pm 2.0 mph. The

		•		
	Ð			

value used for the standard deviation of the population, σ , had to be determined from a pilot study since there were no recent data available.

The pilot study was conducted in West Lafayette,
Indiana on Northwestern Avenue (U.S. 52) between Stadium
Avenue and Lindberg Road, a distance of approximately 1.1
miles. Data were collected for two directions on three
separate Tuesdays in three months in 1970. The license
plate method of data collection was used during the early
afternoon of each day. A fifteen minute period was
allocated to each direction for collection, providing
between thirteen and twenty-five pieces of usable data
for analysis.

The analysis showed that the standard deviation ranged from 1.669 to 4.851 (requiring sample sizes from three to twenty-two). However, the majority of the values were centered around 3.2, producing a sample size of ten. It was at this point that a homogeneity of variance test was conducted to determine whether the six values of σ^2 were equal. A Statistical Program, DATASUM which includes the Foster-Burr Test (Q-Test) was used to determine this (See Appendix A for description of this test). The data passed the Foster-Burr Test. Hence, it was decided to accept the hypothesis that the variances (and standard deviations) were equal. A sample size of ten was then chosen for use in data collection.



Selection of Study Sections

Once the sample size for each section had been chosen (ten observations) it was then necessary to determine the number of cities and the number of sections in each city to be examined.

At the outset of this research project it was decided that the work should be limited to cities whose population ranged from thirty to one hundred and fifty thousand There were two reasons for this decision: economy and expedience. Economy refers to conserving the limited resources of both time and money. This was achieved by restricting the data collection to nine Indiana cities in order to limit the resources expended in traveling between cities. Cities with populations less than thirty thousand were not included because the characteristics of their arterial streets are considerably different than such streets in larger cities, i.e. the fringe area is very small or non-existent, homogeneous street sections are very short, and traffic engineering is often not used. The ground for not examining cities over one hundred and fifty thousand population is that they are too few in number (Table 1). According to Table 1 eighty-five percent of all Indiana cities with populations greater than thirty thousand fall within the specified range. At the national level the figures are just as impressive: eighty-three percent of all cities over twenty-five thousand have

all is sampled

TABLE 1
POPULATION GROUPINGS OF CITIES IN U.S.A. AND INDIANA

U.S.A. (1960 Census)		Indiana (1970 Census)	
Number of cities with populations > 10000	1899	Number of cities with populations > 30000	20
Number of cities with populations > 25000	765	Number of cities with populations between 30000 and 150000	17
Number of cities with populations between 25000 and 250000	714		
Number of cities with populations between 25000 and 100000	633		

populations between twenty-five and one hundred thousand, while ninety-three percent of all cities over twenty-five thousand have populations between twenty-five and two hundred and fifty thousand.

In order to economize limited resources and to aid some of the smaller cities of the state by supplying them with study data, it was decided to collect all data within the state of Indiana. After organizing the seventeen cities that were included in the specified range into the three classes it was found that the second and third classes each contained three cities. The decision was then made to use three cities from the first class, thereby creating nine cities to be investigated (Table 2). In Class I the preference of one city over another included consideration of its proximity to Purdue.

Each section investigated was observed under two traffic conditions. The first was the afternoon off-peak and the second was the evening peak period. The evening peak was chosen instead of the morning because it tends to be better defined and greater in magnitude. However, using these two conditions covers most of the spectrum of problem traffic conditions except the possible situations where a two-way street carries high volumes in both directions during the noon lunch hour.

The judgment was made to research ten sections in each city to provide a sizeable number of observations at the



TABLE 2
STUDY CITIES AND THEIR CLASSIFICATION

Class	Population Range	City
I	30000 - 49999	Lafayette Kokomo Marion
II	50000 - 99999	Anderson Muncie Terre Haute
III	100000 - 149999	Hammond South Bend Evansville



completion of data collection.

The choice of streets actually studied was accomplished by visual inspection. In making this judgment three factors were employed. The first was location within the city.

This was restricted to the fringe area of the Central Business District. The second criterion was section length. In chosing the test sections an attempt was made to maintain a minimum length of one half mile; however, this proved quite difficult at times due to the third selection factor, homogeneity. Each street used had to be uniform along the length analyzed in the following four aspects:

- 1. Street Type (i.e. one-way or two-way)
- 2. Parking
- 3. Approach Width
- 4. The Absence of STOP and YIELD Signs in the Section

For the most part, satisfying the above conditions, with the exception of length, was not exceedingly difficult. Of the ninety sections investigated sixty-three percent were one-half mile or longer while slightly over eighty-three percent were 0.45 miles or longer (Figure 1). In the cases where the section length was less than four-tenths of a mile (only seven of ninety sections) the number of major causes of speed reduction, e.g. traffic signals and railroad crossings, was kept to a minimum (usually one) in order to guarantee that the test vehicle

(usually c

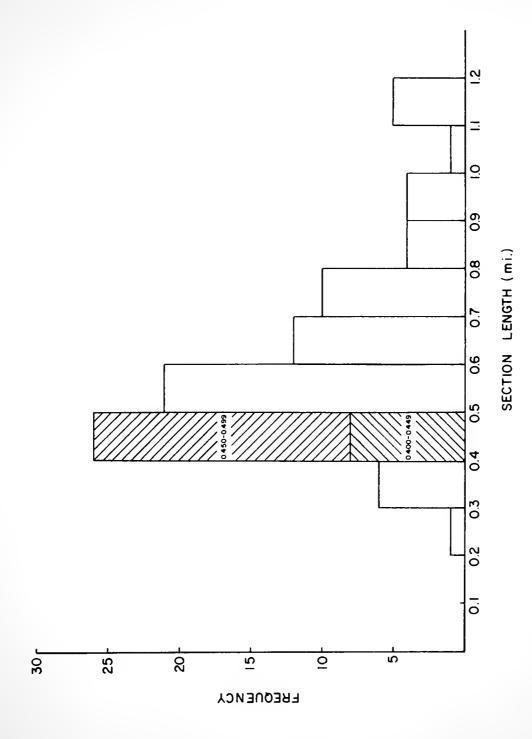


FIGURE I. FREQUENCY OF SECTION LENGTH



could cruise and not merely accelerate and decelerate.

Refer to Table 3 for a listing of the streets selected.

Although ten sections of arterial streets were desired in each of the nine cities, only eight adequate sections could be found in Marion. As a consequence an additional two sections were used in Kokomo, a similar sized city in the same area of the state.

Although the posted speed limits of the sections ranged from 20 mph to 40 mph, less than eight percent of the streets had speeds different than 30 mph. The average speeds on those streets with a posted speed less than 30 mph were found to be about thirty miles per hour, while those streets with a posted speed greater than 30 mph were approximately thirty-five miles per hour.

During the off-peak traffic condition observations were taken on all ninety sections; however, during the peak traffic condition observations were taken on only sixty-two sections. This was a result of the absence of a peak volume on some streets during the evening peak period. In some cases the section was a one-way street of a pair, while in others it was one direction of a two-way street. As a consequence, of the one hundred and eighty conditions that could possibly be investigated only one hundred and fifty-two actually were analyzed.

TABLE 3

SELECTED TEST SECTIONS WITH PERTINENT DATA

City	Street	Sec.	Terminal Points	ά	Length (Mi.)	Peak 15 Min. Vol.	Surround- ing Area Descrip- tion
Lafayette	Union	7	14th	1st Barrel	0.411	309	Res, Com
	Main	6	South	Earl	1.187	158	Res, Com
	Main	11	Earl	South	1.199	110	Res, Com
	Northwestern	35	Lindberg	Stadium	1.097	94	Res
	Northwestern	36	Stadium	Lindberg	1.106	304	Res
	Teal	57	9th	18th	0.486	186	Res, Com
	Teal	28	18th	9th	0.486	196	Res, Com
	Columbia	59	10th	Main	0.298	179	Res
	9th St.	64	Potomac	Virginia	0.477	93	Res
	9th St.	65	Virginia	Potomac	0.484	214	Res
Kokomo	Apperson Way	13	North	Jefferson	0.483	09	Res
	Apperson Way	16	Jefferson	North	0.489	97	Res
	Sycamore	17	Phillips	Webster	0.518	63	Res
	Sycamore	18	Webster	Phillips	0.520	126	Res
	Jefferson	29	Wabash	Korby	0.415	92	Res, Com
							Ind
	Jefferson	30	Korby	Wabash	0.416	09	Res, Com Ind
	Phillips	72	Elm	Walnut	0.555	35	Res, Com
							Ind
	Phillips	73	Walnut	Elm	0.556	113	Res, Com Ind
	Markland	74	Plate	Buckeye	0.885	176	Com
	Markland	75	Buckeye	Plate	0.887	126	Com
	Morgan	68	Apperson Way	Webster	0.476	165	Res, Com
	Morgan	06		Apperson Way	0.476	193	Res, Com

TABLE 3 (Continued)

Surround- ing Area Descrip- tion	Res, Com Res, Com Res Res Res Res Res Res Res Res Ind	Res, Com Res, Com Res, Com Res, Com Ind Res, Com Ind Res Res Res Res Res Res, Com Res Res, Com Res Res, Com
Peak 15 Min. Vol.	249 237 117 197 181 135 246 121	193 229 2294 171 195 134 174 160 180
Length (Mi.)	1.185 1.180 0.441 0.745 0.752 0.634 0.633	0.564 0.681 0.718 0.717 0.364 0.359 0.646 0.646
ts	Cross Grand Lowell Silver Brown Henry Van Buskirk 5th	l6th Highland Cowing Walnut Lanewood Euclid Burnell Utica Elliot Ohio Monroe
Terminal Points	Grand Cross Silver Lowell Henry Brown 5th Van Buskirk 17th	24th Cowing Highland Lanewood Walnut Burnell Euclid Elliot Utica Madison
Sec. No.	19 20 22 23 24 25 26	28 33 33 34 44 46 50
Street	Broadway Broadway Cross Cross 8th St. 8th St. Madison Madison Meridian	Main Wheeling Wheeling McGalliard McGalliard Tillotson Tillotson Memorial Memorial Jackson Main
City	Anderson	Muncie



TABLE 3 (Continued)

City	Street	Sec. No.	Terminal Points	ts	Length (Mi.)	Peak 15 Min. Vol.	Surround- ing Area Descrip- tion
Terre Haute	Poplar	37	22nd	12th	0.843	104	Res, Com
	Poplar	38	12th	22nd	0.838	185	Res, Com Ind
		39	Maple	6th	0.625	102	Res, Ind
	13th St.	40	6th	Maple	0.625	132	Res, Ind
		41	8th	Maple	0.498	84	Res
	25th St.	42	Maple	8th	0.496	91	Res
	a.	43	25th	15th	0.741	57	Com, Ind
	Maple	44	15th	25th	0.747	62	Com, Ind
	Ohio	62	13th	18th	0.428	195	Res
	Walnut	63	18th	13th	0.426	107	Res
Marion	Wabash		Kem	Quarry	0.516	120	Res
	Wabash	52	Ouarry	Kem	0.516	147	Res
	Washington		McKinley	Grant	0.550	138	Res, Com
	Washington		Grant	McKinley	0.547	158	Res, Com
	Washington		11th	26th	0.937	176	Res,Com
	Adams		26th	llth	0.936	184	Res,Com
	שׁ		Baldwin	Geneva	0.389	142	Res,Com
	W. 2nd St.	19	Geneva	Baldwin	0.397	115	Res, Com



TABLE 3 (Continued

City	Street	Sec.	Terminal Points	v	Length (Mi.)	Peak 15 Min. Vol.	Surround- ing Area Descrip- tion
South Bend	Sample Sample Edison Edison Portage Portage Jefferson Jefferson Washington	66 67 69 70 71 81 83	Camden Edison Beutter Pyle Bergan Queen Jacob Ironwood Laurel	Edison Camden Pyle Beutter Queen Bergan Ironwood Jacob Birdsell	0.758 0.535 0.535 0.636 0.646 0.476	219 172 160 143 92 105 126 91	Com, Ind Com, Ind Res Res Res Res. Res, Com
Hammond	Columbia Columbia 165th St. 165th St. Kennedy Kennedy Summer	11 12 12 13 14 15 15 16 16 16 16 16 16 16 16 16 16 16 16 16	Kenwood Drackert Columbia Indianapolis 173rd 169th Hammond Valve	Drackert Kenwood Indianapolis Columbia 169th 173rd Berkley	0.547 0.996 0.997 0.492 0.729	1 3 3 5 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4	Res, Com Res, Com Com, Ind Com, Ind Com Rom Res, Ind
	Michigan Michigan		Driveway 2416 Indianapolis		0.561	150	Ind

TABLE 3 (Continued)

City	Street	Sec. No.	Terminal Points	W	Length (Mi.)	Peak 15 Min. Vol.	Surround- ing Area Descrip- tion
Evansville	Franklin	Н	Oakley	Main	0.511	140	Res, Com
	Franklin	7	Main	Oakley	0.501	103	Res,Com
	Garvin	m	Franklin	Louisiana	0.571	124	Res,Com
	Governor	4	Missouri	Illinois	0.571	283	Res,Com
	Washington	ഹ	Kentucky	Lodge	0.491	241	Res
	Washington	9	Lodge	Kentucky	0.481	134	Res
	Columbia	œ	3rd Š	6th	0.326	181	Res,Com
	Columbia	10	7th	Wabash	0.446	140	Res
	Columbia	12	Wabash	7th	0.451	114	Res
	Columbia	88	6th	3rd	0.321	157	Res,Com

			,

Data Collection Procedures

The data that were collected for this project may be divided into three general categories: 1) speed-delay data, 2) volume data, and 3) section inventory data. A section refers to either a one-way street or one direction of a two-way street.

The initial step of research in a city was the obtainment of a city street map and the labeling of the perimeter of the Central Business District (CBD) and the arterial streets. This was usually done by contacting the City Traffic Engineer; however, in some cases it was necessary to speak to either the Police Traffic Officer or the City Engineer. This also proved to be a good opportunity to speak to either the Chief of Police or the Police Traffic Officer and inform them of the type of study that was to be done.

Once the preliminaries were complete the actual data collection began. This required driving to the CBD perimeter and checking each arterial for length and homogeneity. The former was done using a vehicle equipped with a calibrated Stewart-Warner Survey Speedometer (Odometer) while the latter was accomplished by answering the pertinent questions of the Inventory Questionnaire (Figure 2). The remainder of the questionnaire was completed at the researcher's convenience.

Inventory Questionnaire

Check the appropriate spaces		
City		
Street Name		
Type of Street	One-Way	Two-Way
Parking	No Parking	
	Parking (one s	ide)
	NESW	side of street
	Parking (both	sides)
Number of Railroad Crossings		
Number of Driveways	Commercial	Private
Section Direction	North	East
Approach Width		
Lane Markings	Yes	No
Section Direction	South	West
Approach Width		
Lane Markings	Yes	No
Number of Signalized Intersections		
Number of Intersections Other than Signalized		
Number of Alleys		
G/C Ratios		
Intersecting Street	G/C Ratio	



After a street was chosen, Streeter Amet Trafficounters (Models RC or RCT) were installed in each direction. These pneumatic tube traffic volume counters were placed so that the volume that passed that point was representative of what travelled on the whole section.

Upon completion of this phase a speed-delay study was begun, using the average car method. In brief, this method involved one of the researchers driving the test vehicle along the section at what he considered the average speed of the traffic stream while simultaneously measuring, using a stop watch, the total time of the trip. At the same time, a recorder timed all stops and noted both these and other forms of delay. The data sheet completed by the recorder is shown in Figure 3. Upon returning to the office the researcher completed the data sheet and proceeded to complete the Summary Sheet (Figure 4).

This procedure was followed on each run with ten runs performed under two traffic conditions on each section, during the off-peak period and again during the evening peak period. To determine the time and magnitude of the peak period a traffic volume counter was left in position for twenty-four consecutive hours between Monday and Friday. However, this method had to be modified on many sections due to equipment malfunction or damage to the pneumatic tubing by street cleaning equipment. The modification applied was the installation of the traffic

TRAVEL TIME STUDY

		TRIP NO.					
ROUTE			DIRE	DIRECTION			
TRIP STARTED AT				ION M			
REFERENCE S'		STOPS		SLO	NS		
POINT	TIME	LOCATION	CAUSE	DELAY SEC.	LOCATION	CAUSE	
TOTAL 3	rrip Tin	ME	TOTAL	TRIP LE	NGTHOVI	ERALL SPEE	
DIINNTN	C TTME		STOPPED	TIME	RUI	NNING SPEE	

FIGURE 3. DATA SHEET FOR TRAVEL TIME STUDY

DATE _____ WEATHER ____



Summary Sheet

Summary brieec							
Route				Len gt h	· · · · · · · · · · · · · · · · · · ·		
Betwee	en			And			
Date .	· · · · · · · · · · · · · · · · · · ·	Time	AM _PM to	AM PM			
Major	Cause	for Delay	Trip No.	No. Times Stopped	Total Sec. Stopped	No. Times Slowed	Ave- rage Speed
			; 				
			1	I	I	1	1

Date	Compiled By	

FIGURE 4. SUMMARY SHEET FOR TRAVEL TIME STUDY

TOTALS

AVERAGES PER TRIP

volume counter during the late morning hours and the removal of it the same day during the early evening hours.

If this type of study is to be a success the people being observed must not know what is taking place. The test vehicle is important in this matter. The vehicle used for the data collection was a 1962 Chevrolet four door sedan; in no way was the vehicle conspicuous.

The Inventory Questionnaire (Figure 2) was the only original form used in the study, the others being standard forms from the Manual of Traffic Engineering Studies (10). It functioned as a substitute for a condition diagram of the section using both qualitative and quantitative questions. All the required measurements could be completed by one person with the exception of that of the approach width. Usually three width measurements were taken, one at each end and one in between, using a metallic tape. The G/C ratios were usually supplied by the City Traffic Engineer; however, in cases where they were not, the measurements were made and the percentages rounded to the nearest integral number.

An inherent problem in the average car method arose in data collection. During off-peak measurements there were periods when the test vehicle was not included within visible range of other vehicles. The driver of the test vehicle then had to make the decision of choosing a speed that he felt was average. To wait outside the section for

other vehicles usually does not alleviate the problem - all too often under low volume conditions a group of other vehicles does not materialize. It was sometimes difficult under such conditions for the driver of the test car to be certain he drove at the speed of the average vehicle.

The bulk of the data collection was done between February and May of 1971 and only during dry weather conditions. It should also be noted that the data was collected on weekdays, with the exception of one Saturday afternoon.

DATA ANALYSIS

Original Variables

Table 4 is a listing of the variables used in the development of the model. Of the twenty-two variables investigated, only eleven are actually included in the proposed model. It should also be noted that one of the twenty-two variables, Driver, was added just prior to the choosing of the model. This was done to try to improve the model, but which it did to only a very small degree.

Information for many of the variables was obtained directly from the Inventory Questionnaire. Data for the twenty first variable, Progression, however, resulted from value judgments on the part of the researcher. Value judgments present difficulties because other researchers might have made different decisions. In the case of a section where there were zero or one signalized intersection, the section was considered to have good progression. Where the section had more than one signalized intersection, the researcher on the basis of speed progression actually obtained during the runs made the judgment as to whether or not good progression was present.

The twenty-second variable, Driver, represents whether Driver A or Driver B was at the wheel of the test vehicle.



TABLE 4

VARIABLES TESTED IN DEVELOPMENT OF THE MODEL

Variable Number	Variable Name	Description and Information Coded
1	Running Speed	The length of the section divided by the time in motion for one trip along that section (mph).
2	Peak	Denotes whether measurements were done during the P.M. Peak period or not. Off-Peak = 0 P.M.Peak = 1
3 (A)	Section Length	The length of the section in miles.
4	Street Type	Denotes whether the section is a one- or two-way street. One-way = 0 Two-way - 1
5 (B)	Approach Width	The curb to curb width (face of curb) in feet for one-way streets and the curb to centerline width in feet for two-way streets.
6	Lane Marking	Used for multilane facilities only. No = 0 Yes = 1
7 (C)	Signalized Inter.	The number of signalized inter- sections included in the section.
8 (D)	Unsignal- ized Inter.	
9 (E)	Alleys	The number of alleys included in the section.
10	Private Driveways	The number of private driveways included in the section.
11	Commercial Driveways	The number of commercial driveways included in the section.



TABLE 4 (Continued)

Variable Number	Variable Name	Description and Information Coded
12	Day	The day of the week that the data was collected. Sun = 1 Mon = 2
		: Sat = 7
13(F)	Pop.	Denoted the population class 30000-49999 = 0 50000-99999 = 1 100000-149999 = 2
14 (G)	Railroad Crossings	The number of individual crossings (not the number of tracks) included in the section.
15	Parking	Variables 15, 16, and 17 are Parking dummy variables whose relationship is:
16	Parking	15 16 17 0 0 Parking on both sides of the section
17 (H)	Parking	1 0 0 No parking on either side of the section
		0 1 0 Parking on the left side of the section
		(one-way streets) 0 0 l Parking on right side of the section.
18 (I)	Volume	The fifteen minute volume which was concurrently measured with the observation (one trip).
19 (J)	Lowest G/C ratio	The lowest G/C ratio of all the signalized intersections included in the section.
20	Average G/C ratio	The average of all the G/C ratios included in the section.



TABLE 4 (Continued)

Variable Number	Variable Name	Description and Information Coded
21 (K)	Good Progression	A value judgment of whether good progression existed in those sections which contained two or more signalized intersections. No = 0 Yes = 1 (also used for sections with zero or one signalized intersection)
22	Driver	Denotes driver of the test vehicle Driver A = 0 Driver B = 1

Range of Variable Measurements

Variable Number	Range
3	0.298 miles - 1.199 miles
7	<pre>0 traffic signals - 6 traffic signals</pre>
13	30000 people - 150000 people
14	0 crossings - 2 crossings
18	24 vehicles - 354 vehicles
19	25% - 100%
20	25% - 100%



Upon examination of the covariance matrix it was found that one driver drove, on the average, nine-tenths of a mile per hour faster than the other.

A listing of the limitations of the individual variables, where this is relevant, is given at the end of Table 4.

Preliminary Testing

As data collection progressed it was felt necessary to determine if the data indicated a homogeneous population. To accomplish this the Q-Test contained in Statistical Program DATASUM was again employed. Table 5 is a summary of these results, including the results of the tests made at the completion of the data collection stage. The tests made during data collection indicated homogeneity while those made upon completion of data collection indicated heterogeneity. A possible reason for the failures for the data at completion might be the non-normality (see Appendix B) and not the heterogeneity of the data (4).

At this stage of the analysis it was realized that interaction between the variables was quite high and an attempt was made to determine it, using two-way ANOVA tests. Unfortunately, due to the incompleteness of the cells, it was found impossible to perform these tests. Therefore, regression analysis was employed, using cross products to investigate the interaction.

TABLE 5
SUMMARY OF HOMOGENEITY TEST RESULTS

Nu		of Va	ria	nces	5		(Q-T0 0.05	est Level	.)
(Tests	Made	Durin	ıg D	ata	Coll	ect	ion)			
6							P	asse	đ	
12							P	asse	đ	
16							P	asse	đ	
20							P	asse	đ	
24							P	asse	đ	
44							P	asse	đ	
(Tests	Made	Upon	Com	plet	ion	of	Data	Col	lectio	n)
62	(Peak	c)					F	aile	đ	
90	(off-	-Peak)					F	aile	đ	
152	(Tota	a l)					F	aile	d	

	20 (

Stepwise Regression

Towards the completion of the data collection phase, investigation of Statistical Program BMD 2R (Stepwise Regression) (17) began. Using three hundred and sixty observations, different F-ratios and Tolerances were examined for deviation between models created. Due to a lack of deviation in the models the following values were chosen and utilized throughout the analysis: F-ratio = 1.75 and Tolerance = 0.001.

Phase 1

Using a sample of six hundred observations and containing only the first seventeen variables (see Table 4), the input for a model was created. Nine of these variables were chosen for use in forming transgenerated variables, e.g. squares and cross products. These nine variables were:

- 1. Section Length
- 2. Approach Width
- 3. Signalized Intersections
- 4. Unsignalized Intersections
- 5. Alleys
- 6. Railroad Crossings
- 7.-9. Parking Dummy Variables

Those transgenerated variables which were either removed from the model during its development or never entered because of low F-ratios were eliminated from further consideration.

THE TATE OF REPORT

Soon afterwards another two hundred and ten observations were added and the process continued. The logarithms of some of the original variables were also examined during this phase of the regression analysis. Later another three hundred observations were added to the model's input.

Phase 2a

Phase 2a was an attempt at utilizing the most significant variables found from analyses of the eight hundred and ten observations and the eleven hundred and ten observations of the previous phase. At the same time variables concerning volume and traffic signal phasing were added. The input for the Phase 2a models is diagrammatically shown in Figure 5. At the completion of Phase 2a the R² value was 0.6679 for a model containing twenty-nine variables (original and transgenerated).

Phase 2b

Simultaneous to the running of the Phase 2a models

Phase 2b was attempted. The Phase 2b input is shown in

Figure 5. The function of this phase was to check whether

or not the three hundred additional observations of the

eleven hundred and ten observation model had caused certain

variables to become more significant. At the termination

of Phase 2b an R² value of 0.6919 had been reached using

thirty-six variables. Because the final Phase 2b model

17-13/12/10

Appropriate Variables from Logarithms of Groups A, B, C, D, and E Logarithms of Groups A, B, C, D, and E Reciprocals of Groups A, B, C, D, E, and F Group F Group F Group G + + Cross Products
of Groups B
and C Cross Products of Groups B and C The Most Significant Transgenerated Variables Remaining at the Completion of Phase 2b Group F Group E Group E + Group E Squares of Group C Squares of Group C Group D Group D Phase 2b Input Phase 3a Input Group D Original Variables #18-#21 Original Variables #18-#21 Group C Group C + Group C Transgenerated Variables from Transgenerated Variables Models Formed From 1110 Common to Models Formed with 810 and 1110 Observations Observations Identical to Phase 2b Groups Group B Group B Group B + Variables Original Variables #1-#17 Original Group A Group A Group A

Phase 2a Input

FIGURE S. MODEL INPUTS



appeared more promising than its Phase 2a counterpart, it was decided to enter Phase 3a using the most significant variables from the Phase 2b model.

Phase 3a

Phase 3a was based on the same input as Phase 2b except for the addition of the more significant transgenerated variables entered during Phase 2b and the reciprocals of some of the variables. These reciprocals were also used to form new cross products. Although many new transgenerated variables were examined the value of R² remained relatively unchanged.

Phase 4a

Phase 4a was the stage in which illogical transgenerated variables were removed from the model. In
addition to the twenty-one original variables, another ten
logical (logical in individual effect) variables were
selected from the most significant transgenerated variables
entered into each of five Phase 3a models. It was from
this phase that the final prediction model was developed.

The Prediction Model

The model that was chosen contains ten terms and utilizes eleven original variables. It represents the Phase 4a model where each term increased the value of R² by approximately one percent. The model is shown below in



test format, followed by the Summary Table from the stepwise regression program (Table 6).

$$\hat{Y} = 19.62500 + 10.38018X_3 + 0.07562X_5 - 0.70139X_7$$

$$- 0.22178X_8 + 1.25800X_{13} - 0.03118X_{18} + 7.38855X_{19}$$

$$- 0.18590X_{22} - 0.24199X_{23} + 0.01815X_{24}$$

where

Y = predicted average running speed

$$x_{22} = \frac{x_8 x_{14}}{x_3}$$

$$x_{23} = \frac{x_9 x_{17}}{x_3}$$

$$X_{24} = X_{18}X_{21}$$

See Table 4 for definitions of all other variables.

In Chapter 3 of Draper and Smith (2), "The Examination of Residuals," it states:

We can see that ... the residuals e are the differences between what is actually observed, and what is predicted by the regression equation — that is, the amount which the regression equation has not been able to explain. Thus we can think of the e as the observed errors if the model is correct. Now in performing the regression analysis we have made certain assumptions about the errors; the usual assumptions are that the errors are independent, have zero mean, a constant variance, σ^2 , and follow a normal distribution.

Appendix C contains the frequency plot of the residuals and the Kolmogorov-Smirnov Test for normality. The frequency plot looked normal and the test accepted the

frequen

TABLE 6

STEPWISE REGRESSION SUMMARY TABLE

Variable Entered	Multiple R	e R2	Increase In R ²	F Value to Enter Or Remove	Standard Error of Estimate
0.5159	6	0.2661	0.2661	550.5366	4.5772
0.5951	_	0.3541	0.0880	206.5654	4.2909
0.6504	_	0.4230	0.0689	180.9292	4.0570
9689.0	10	0.4755	0.0526	151.7938	3.8692
0.7095	10	0.5034	0.0279	0660.88	3.7660
0.7297	~	0.5324	0.0290	93.7886	3.6557
0.7458		0.5562	0.0238	80.9227	3.5628
0.7532	~ 1	0.5673	0.0112	39.0363	3,5188
0.7532	01	0.5673	-0.0001	0.2747	3.5180
0.7594	₹1"	0.5767	0.0095	33.7673	3.4805
0.7635	Ŋ	0.5829	0.0062	22.2784	3.4562
0.7698	œ	0.5926	0.0097	35.8412	3.4170

A minus sign means that the variable was removed. * Note:

		•
Ĭ.		

hypothesis at a significance level of 0.05. The mean of the residuals was zero. To test the independence of the residuals two different approaches were used, neither producing favorable results. Each approach used a different ordering of the "runs" test outlined in Draper and Smith (2). The first ordering was a time approach. This was done by chronologically ordering the residuals of ten randomly chosen workdays. The results produced, however, were unsatisfactory. The ordering of the predictions (from lowest to highest) and their corresponding residuals was the second approach. Again, the results were the same.

A study of the plot of the residuals and the observations (running speeds) showed that as the speeds approached the limits of the observation range, the residuals tended to be of one sign. Therefore, if a chosen speed were at either extremity all the residuals would be of one sign, independent of time ordering. Because all speeds taken during a single workday were on only a few sections, the chosen runs on a single workday (the basis of this ordering approach) tended to have similar speeds, sometimes at one of the extremities.

In many instances, residuals are ordered with respect to one of the independent variables. This was not possible in this study because the variables were discrete over a narrow range. In place of one of the independent variables,

A

17.4

A DESCRIPTION OF THE PROPERTY OF

the prediction Y had to be used. This approach did not prove independence because the ordering from lowest to highest provided large groups of residuals of similar sign.

Though the tests to determine whether or not the residuals were independent failed, there may be good reasons for this result. The test used is most sensitive to independence for models of excellent fit. The model tested explains about sixty percent of the variation of the total sums of the squares of the running speed. Finally, as already noted, the ordering choices for which the residuals were tested presented difficulties.

The multiple correlation coefficient (R^2) for the model is 0.5926. There are three basic reasons why this value is not higher. The first reason is that the number of terms appearing in the model was kept to a minimum for calculation ease. Adding another ten terms would have raised the value of R^2 by only another six percent and some of these were not individually logical. It should be noted that the highest value of R^2 achieved during the analysis was 0.7022 using a model containing forty-two terms.

The second and probably the most important reason is the variability of drivers in the traffic stream. Many of the factors that influence a driver's actions are known but cannot be measured either quantitatively or qualitatively. To give some examples: 1) motivation

The Language

factors, such as attitude; 2) emotional factors, such as anger and fear; and 3) other modifying factors, such as fatigue, climate, and time of day. Motorists who are fatigued and inattentive drive differently than they normally would and some may even try to compensate for these factors. Unfortunately, in making this type of study the researcher has great difficulty determining which of these factors are influencing (or to what extent) the drivers in the traffic stream which he is studying.

The final reason is variability due to the method of data collection - the average car method. Late in the analysis stage the question of variability between the two test drivers arose. The twenty second variable, Driver, was then created to examine this. First, it was tested in a stepwise regression program with the original variables and proved to be more important than some of them. This new variable was tested with the terms of the final model. The result of this test was a negligible improvement in the explanation (R²); therefore, it was not included. Another reason for this method's variability is the already discussed difficult driver selection of an average speed under low volume conditions.

After the selection of the model the decision was made to test it using part of the data collected. Ten of the sections were chosen from the data by randomly ordering peak and off-peak conditions, then randomly



ordering the section numbers and matching the first ten of each. The model was tested with coefficients to five places and the coefficients rounded to three places. Since the results were adequate for both coefficient conditions (Table 7), it was decided to use the model with rounded coefficients to simplify calculation.

To determine the accuracy of the model as a predictor, the standard deviation of each prediction, S, was estimated. The value of S, could be calculated using an equation similar to the equation for the one independent variable case, shown below:

$$s_{\hat{Y}}^2 = s_{E}^2 \quad \left[1 + \frac{1}{n} + \frac{(X - \bar{X})^2}{\sum_{x} x^2}\right]$$

where

X = the independent variable

$$x = x - \bar{x}$$

The assumption was made that the third term in brackets was small and it was known that 1/n (1/1520) was very small, so that

$$s_{\hat{\mathbf{v}}}^2 \approx s_{\hat{\mathbf{E}}}^2$$

The standard error of the estimate (3.417) then approximates the actual value of $s_{\hat{a}}$.



TABLE 7

RESULTS OF TESTING THE MODEL

Predictions of Model Utilizing Three Place Coefficients (mph)	22.313	27.141	32.054	28.880	28.570	27.776	29.291	29.577	33.374	31.936
Prediction of Moutiliar Three Coeff (mph)	22.	27.	32.	28.	28.	27.	29.	29.	33.	31.
Predictions of Model Utilizing Five Place Coefficients (mph)	22.310	27.132	32.044	28.871	28.563	27.770	29.281	29.562	33.363	31.921
Average Speed of Observations (mph)	22.792	24.508	29.534	28.022	24.239	30.316	26.341	30.532	35.128	31.720
City	Kokomo	Muncie	Anderson	Terre Haute	Terre Haute	Marion	Terre Haute	South Bend	South Bend	Anderson
Street Name	Morgan	Wheeling	Cross	25th St.	Poplar	Wabash	25th St.	Jefferson	Edison	Broadway
Peak Period	No	Yes	No	No	No	No	Yes	No	Yes	Yes
Sect.	89	31	22	41	37	51	42	. 08	89	20



TABLE 7 (Continued)

Predictions	Utilizina	Three Place	Coefficients	(mph)
	Utilizing	Five Place	Coefficients	(mph)
	Average	Speed of	Observations	(mph)
				City
				Street Name
		•	Peak	Period
			Sect.	No.

Whose Deviation Were Included in the + 2 mph Number of Predictions Range

Ŋ Ŋ

Average Deviation From The Average of the Section Observations

1.923 1.921

the Average of the Section Maximum Deviation from Observations

4.332 4.324



The model in its final form using alphabetical subscripts is shown below.

$$\hat{Y} = 19.625 + 10.380X_A + 0.076X_B - 0.701X_C$$

$$- 0.222X_D + 1.258X_F - 0.031X_I + 7.389X_J$$

$$- 0.186X_DX_G - 0.242X_EX_H + 0.018X_IX_K$$

where

$$X_A = X_3$$

$$X_B = X_5$$

$$x_{c} = x_{7}$$

$$x^D = x^8$$

$$X_E = X_9$$

$$x_F = x_{13}$$

$$x_G = x_{14}$$

$$X_H = X_{17}$$

$$x_{I} = x_{18}$$

$$X_J = X_{19}$$

$$X_K = X_{21}$$

Though eleven variables were entered into the model, eleven others were not. It might be of interest to examine some of them now. Proceeding in the order of significance, the next variable that would have been

entered was Street Type (one-way or two-way) the coefficient of which was illogical. Surprisingly enough, the variable which denoted whether or not the prediction was being made for the peak condition entered into the model very late in the analysis, indicating a lack of significance, and had a small coefficient. Another variable which originally was hypothesized as being influential was Commercial Driveways. This variable also entered the model late in the regression analysis.

						-

ANALYSIS OF STOP DELAY

The prediction of average running speed is a reasonable means of determining and evaluating some of the causes of speed reduction; however, to justify where and what improvements should be made it is usually necessary to have knowledge concerning any stop delay time. This section will be devoted to pointing out those locations where stop delays occurred in this study and their average values. Equipping the traffic engineer with both a running speed prediction model and average stop delay data will enable him to estimate where improvements should be made and the total benefits accrued therefrom.

A major part of this study was devoted to the measurement of stop delay, i.e. the time elapsed while the test vehicle was at a complete stop. On the sections investigated in this research project these stop delays were caused by three different factors:

- 1. Traffic Signals
- 2. Railroad Crossings
- 3. Miscellaneous Delays

Utilizing the data from this study, it was found that Traffic Signals had the greatest influence on stop delay

for both the off-peak and peak condition. For the off-peak condition the percentage of the total stop delay attributed to each factor was as follows: 81.90%, Traffic Signals; 15.50%, Railroad Crossings; and 2.60%, Miscellaneous Delays. During the peak period the same factors had values of 84.91%, 12.47%, and 2.62%, respectively.

Miscellaneous Delays contains any other causes of stop delay except by traffic signals and railroad crossings; however, during this study it was produced by left turns, right turns, school crossings, stopped vehicles in the roadway, and pedestrians crossing the roadway. The major and most common delay producing element of this factor was the left turn (36.80% of this factor's stop delay during the off-peak period and 74.90% during the peak period).

Tables 8 and 9 contain the delay data collected during the study. Table 8 is a tabulation of the off-peak data while Table 9 is a tabulation of the peak data. The delays recorded are the averages of the stop delays encountered during the ten observations along each section for each condition. Within Miscellaneous Delays the delays have been presented as the average delay per mile as opposed to the localized effects of Traffic Signals and Railroad Crossings.

A listing of the important statistics developed from the stop delay data is shown in Table 10.

TABLE 8

AVERAGE DELAY TIME PER SECTION (SECS)

((misc. Delays Per Mile				1.09	2.29												
2	E D D4	0	0	0	٦	2	0	0	0	0	0	0	0	0	0	0	0	0
Bailroad	Crossings 1 2	0							23.97			0	0			0	0	0
	9																	
Off-Peak	Traffic Signals 3 4 5		24.52	34.15								4.80	19.09			11.60		18.43
	1 2	16.30			6.59	5.43	23.23	0.70							8.30	11	10.68	
	0								0	0	0			0				
	Section	7	6	11	35	36	57	58	59	64	65	13	16	17	18	29	30	72

TABLE 8 (Continued)

	, N	misc. Delays Per Mile		0	2.92	0.65	0	0	0	0	0	0	1.88	0	0	0	0	3.01	0	0	2.55	1.35
	Dailroad	Crossings	1	0	33.60	0	0.42	0	0	0	14.81	0	0	0			0	0			1,65	10.75
		Ç				20.99																
		Ŋ)		12.63																	
14 950	OII-Peak	Signals																9.99				
		Traffic 8	1	13.73				15.29	3.88	7.84			16.48	15.29			16.40	6	11.03	10.80		
		-	ļ				8.01								4.79	7.12					6.62	
		0									0	0										0
		Section		73	74	75	68	06	19	20	2.1	22	23	24	25	26	27	28	31	32	33	34

			. 4

TABLE 8 (Continued)

۸s	Mile																			
Misc. Delays	Per	0	0	1.11	0	0	0	0	0	0	0.32	0	0	0	0	0	0	0	1.47	0
Railroad Crossings	1 2									43.88	0			10.22	2.55					
	9																			
als	ß																			
igan	3 4							5.38	13.47											
Traffic 8	2			12.93	15.70						24.58						13.59			
	п					3.17	9.72			5.98		7.39	0.98		13.20	0		5.90	6.45	8.62
	0	0	0											0						
coction	Number	45	46	47	48	49	50	37	38	39	40	41	42	43	44	62	63	51	52	53

TABLE 8 (Continued)

7.7	Misc. Delays Per Mile	0	0	2.21	0	0.76	0	0	0	0	0	0	0.54	0	2.42	10.01	0	0	0	0
ָרָ 	Crossings		0	0																
	9																			
¥	S																			
Off-Peak	ic Signals												2.45							
	Traffic 3													0			11.12	8.38		
	н	3.73	0			17.74									5.72	4.44			29.20	39.66
	0			0	0		0	0	0	0	0	0								
	Section Number	54	55	26	09	61	99	29	89	69	70	71	80	81	82	83	14	15	92	77

TABLE 8 (Continued)

	Railroad Misc. Crossings Delays 5 6 l 2 Per Mile	0	0	0	0	0	0	1.31	0	0	0	0 0	0 0	0	0	0	
Off-Peak	Traffic Signals	10.76	10.77		0	8.67		7.75	12.99	7.02	15.26	2.64	15.47	11.89	11.95		
	0			0			0									0	ć
	Section	78	42	84	85	86	87	1	2	ж	寸	2	9	&	88	10	(

TABLE 9

AVERAGE DELAY TIME PER SECTION (SECS)

	Misc. Delays Per Mile	0	0.27	0	0	2.16	0	0	6.22	0.76	0	0	1.53	0	0	0	0.49	0
	Railroad Crossings 1 2	12.77					0		0	0		0	0	0	0	0	0	0
	9																	
Peak	Ŋ																	
Pe	Traffic Signals 2 3 4		35.60						16.14	17.00		17.67		20.54	9.39	14.19		
	7	23.63		7.84	36.88	10.03					8.41		13.94					
	0						0	0									0	0
	Section Number	7	6	36	57	58	59	65	13	16	18	73	89	06	19	20	21	22



TABLE 9 (Continued)

;	Misc. Delays Per Mile	1.07	88.9	0	0	0	1.69	0.91	0	2.06	0	0	0	0	0	0	0	0	0	0
	Kallroad Crossings 1 2	0	0		25.60	0			16.70	31.43							26.48			
	9																			
	ហ																	\$		
Peak	Traffic Signals 2 3 4	21.93	28.00		10.69	23.68	8.65	52.92					12.18			17.30	16.64			
	-			5.96					8.57					12.92	12.36			8.43	4.45	0
	0									0	0	0								
	Section Number	23	24	25	27	28	31	32	33	34	45	46	48	49	50	38	40	41	42	62

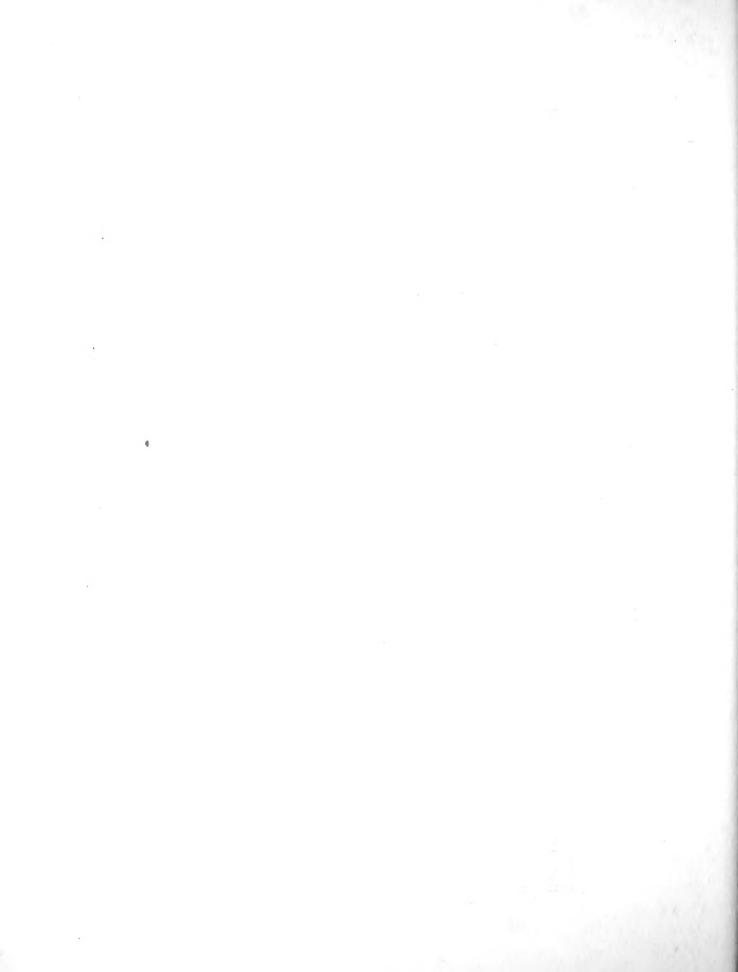


TABLE 9 (Continued)

Peak

Section			Traffic Signals			Railroad Crossings	Misc. Delays
Number	0	7	2 3 4	2	9	н	Per Mile
63			5.32				0
51		11.38					0
52		4.01					0
53		13.05					3.64
54		16.06					0
09	0						0
29	0						0
89	0						0
69	0						0
71	0						0
82		5.88					0
15			13.92				2.63
77		83.29					0
79			24.79				8.56
84	0						0
85		3.56					0
98		21.77					0
87	0						0
J			26.31				0

		·

TABLE 9 (Continued)

Peak

Section	c	-	Traf	Fraffic Signals	gnals	u	ų	Rail Cros	Railroad Crossings	Misc. Delays	
Ta Company	>	4	7	n	r	n	0	⊣	7	rer mile	
2			10.57	7						0.88	
4				14.87	87					0	
Ω.		10.57						0		0	
80		17.09								0	
88		10.89								2.40	
10	0									0	
12	0									0	

TABLE 10

	AVE	AVERAGE DEL	AYS DUE A	DELAYS DUE TO TRAFFIC SIGNALS, RAILROAD CROSSINGS, AND OTHER FACTORS (SECS)	GNALS, F RS (SECS	RAILROAD	CROSSIN	igs,	
				Off-Peak Condition	ition				
	0	-	Tr.	Traffic Signals	Ŋ	9	Railroad Crossings 1	ad .ngs 2	Misc. Per Mile
Average Delay	0	9.13	11.91	14.12	12.63	20.99	3.98	7.73	0.40
Number of Sections	22	34	21	11	1	г	24	9	06
Standard Deviation	0	8.43	5.05	9.55	0	0	8.20	13.28	1.25
				Peak Condition	ion				
	0	1	Tr 2	Traffic Signals 3 4	2	9	RR Xings 1	ıgs 2	Misc. Per Mile
Average Delay	0	14.62	17.83	21.56			5.14	25.60	0.68
Number of Sections	16	24	15	7			17	-	62
Standard Deviation	0	16.19	11.60	7.50			10.25	0	1.69



The delay encountered at traffic signals was found to increase as the number of signals increased and as the condition changed from off-peak to peak. Due to the small number of observations involving sections containing four or more signals analysis was limited to those sections containing one, two, and three signals. During the offpeak period the average delay caused by a single signal was about nine seconds while the delay of a section which contained three signals was found to be approximately fourteen seconds. For the peak condition the respective values were approximately fourteen and one-half seconds and twenty-one and one-half seconds. If each condition is examined individually it is found that as the number of traffic signals per section increased the individual effect of each decreased. During the off-peak period the individual effect for one, two, and three signals is 9.13, 5.95, and 4.71 seconds, respectively. Similarly, for the peak period the delays are 14.62, 8.93, and 7.18 seconds, respectively. Intuitively this reflects the effect of those sections which exhibited good progression. standard deviations that were calculated tend to emphasize the effect of the few signals where the delay for each observation was large because the intersection capacities were exceeded. It was at these intersections that the driver waited through as many as three and four total cycles, whereas at the more typical traffic signal the



wait was only through a portion of a complete cycle. This situation clearly indicates that whenever one is dealing with the condition where the intersection is operating at above capacity, a stop delay study at the particular location will be necessary to obtain accurate estimates of stop delay time.

The average delays encountered in sections which contained one or two railroad crossings (not tracks) were also calculated (Table 10). The standard deviations indicate a high degree of variability in the stop delay. Though a railroad crossing may exist, the number of times that one is delayed is often very few. This is dependent on the frequency that railroad stock uses the particular crossing. Furthermore, if a crossing is blocked, the stop delay of the motorist is dependent on the length and speed of the train. In some cases individual delays at railroad crossings in this study were as long as four or five minutes. To generalize about the magnitude of stop delays at railroad crossings is virtually impossible. It is realistic to conduct individual delay studies at the particular crossings in question to determine these data.

The delays due to the Miscellaneous Delays factor for the off-peak and peak periods were both very small, 0.40 and 0.68 seconds per mile, respectively.

The application of estimated average stop delay values will be most useful in determining and presenting benefits



of traffic engineering improvements. The average values of delay found in this study when utilized according to the restrictions noted enables an estimate of the benefits gained by particular improvements, e.g. constructing a parallel route with fewer traffic signals, the prohibition of left turns or the utilization of one street over another. These benefits could be measured in terms of either time or its chosen money equivalent. The findings also emphasize the fact that the number of traffic signals should be kept to a minimum and that good progression is essential to minimizing stop delay time. A third application of these values might be to point out those sections or intersections which are operating above capacity by contrasting actual delays with the average values found in this study.

CONCLUSION

The primary objective of this project was to formulate a model for predicting the average running speed on urban arterial streets. This has been fulfilled within specified limits of city size and area within the city. From this project comes knowledge of the interaction between frictional factors influencing the motorist and of those frictional factors that most affect him.

The model in its final form is:

$$\hat{Y} = 19.625 + 10.380X_A + 0.076X_B - 0.701X_C$$

$$- 0.222X_D + 1.258X_F - 0.031X_I + 7.389X_J$$

$$- 0.186X_DX_G - 0.242X_EX_H + 0.018X_IX_K$$

where

 X_{A} = Section length in miles

 X_{R} = Approach width in feet

X_C = Number of signalized intersections

X_D = Number of unsignalized intersections

 $X_{F} = Number of alleys$

 X_F = Population class (30,000 to 50,000 = 0; 50,000 to 100,000 = 1; 100,000 to 150,000 = 2)

 $X_C = Number of railroad crossings$



- X_H = Whether or not parking is allowed on the right side of section (No Parking = 0; Parking = 1)
- X_I = The fifteen minute volume in number of vehicles during the time the speed is desired
- X_J = Lowest G/C ratio of all the signals included in the section
- X_K = Whether or not good progression of signals
 exists (No = 0; Yes = 1).

Refer to Table 4 for exact definition of each variable and for the limitations.

Although the coefficient of multiple determination (R²) was not as high as might be desired and although difficulties were encountered in the testing of some of the assumptions, it is believed that the model as a predictor has merit. Estimates of average running speed within a few miles per hour of the true value will be sufficient for most planning and traffic engineering uses. The proposed model has a standard error of estimate of 3.417 mph. For ten examples the model estimated the average running speed within approximately four miles per hour and estimated fifty percent of the values within two miles per hour.

As one reads the list of variables utilized in the model it becomes noticeable that some of these input variables are identical to ones used in capacity calculations. This is what was desired at the outset of the project.

entering and

It is of interest to evaluate the individual effects on average running speed of the variables. Section length affects this speed more than any other variable. The difference in running speed between two sections whose only difference is a half mile in length is about five miles per hour. A variable which substantially affects running speed is volume. The speed is reduced 1.3 mph for every one hundred vehicle increase. Moreover, if a section contains more than one signalized intersection with poor progression, the reduction increases to 3.1 mph for the same number of vehicles.

The population of the city increases the speed to a greater extent than anticipated. For every fifty thousand people increase the speed correspondingly increases 1.3 mph, emphasizing the fact that people drive faster on this type of facility in larger cities.

An important fact contained in the model is that small differences in the lowest G/C ratio produce substantial differences in the speed. As an example, a section whose lowest G/C ratio is 0.50 would have a predicted speed seven-tenths of a mile per hour slower than a section whose lowest G/C ratio is 0.60. The approach width of the section also substantially affects the average running speed. The difference in speed between a section having a twelve foot approach width and a second section having a twenty-four foot approach width is nine-tenths of a mile per hour.

Soci Jopi

The addition of a traffic signal within a section decreases speed by about one-half mile per hour over that existing before installation of the traffic signal. A further reduction results if there are two or more signals in the section and the progression is unsatisfactory.

Table 11 is a summary of this paragraph.

To supplement the usefulness of the proposed prediction model, the stop delay data collected was also analyzed. This research project found the major cause of stop delay to be the traffic signal. In this study the second most important cause of stop delay was due to railroad crossings. These delays increased as the number per section increased for both the traffic conditions of off-peak and peak. The percentage of the total stop delay caused by traffic signals was eighty to eighty-five percent while the percentage caused by railroad crossings was twelve to fifteen percent. Stop delay due to other causes was less than three percent.

Considering sections which contained one traffic signal, the average stop delay was 9.13 seconds during the off-peak period and 14.62 seconds for the peak period. Other sections containing three traffic signals had average stop delays of 14.12 seconds and 21.56 seconds, respectively.



TABLE 11
SUMMARY OF SPEED INFLUENCING FACTORS

Variable Name	Variable Increase	Speed Change
Section Length	0.1 mile	+ 1.0 mph
Approach Width	12 feet	+ 0.9 mph
Signalized Inter.	l unit	- 0.7 mph
Unsignalized Inter.	l unit	- 0.2 mph
Population	50000 people	+ 1.3 mph
Volume	100 vehicles	- 3.1 mph (poor progression)
		- 1.3 mph (good progression)
Lowest G/C Ratio	10 percent	+ 0.7 mph

Using both the prediction model for average running speed and the average values of stop delay enables one to determine the location and extent of improvements to the travel time and to estimate the benefits gained from them. Comparing the benefits with the costs could indicate whether or not the proposed improvement was worthwhile. Alone, the prediction model would function as a means of determining which frictional factors are reducing speed and to what degree so that corrections might be made. Another function of the model would be the determination of appropriate speed limits on urban arterial streets. Hopefully, the knowledge contained in this report will be put to use in the field of traffic engineering.



BIBLIOGRAPHY

- 1. Campbell, E. W., Keefer, L. E., and Adams, R. W., "A Method for Predicting Speeds Through Signalized Sections." H.R.B. Bulletin 230, (1959).
- Draper, N. R. and Smith, H., <u>Applied Regression</u> Analysis. New York: John Wiley & Sons, Inc., 1966.
- 3. Edwards and Kelcey, Inc., "Optimizing Flow on Existing Street Networks." Highway Research Board, N.C.H.R.P. Project 3-14, (1969).
- 4. Foster, L. A., Testing for Equality of Variances. Diss. Purdue 1964.
- 5. Greenshields, B. D., "Measurement of Highway Traffic Performance." Traffic Engineering, XXXIX (April 1969), 26-30.
- 6. Greenshields, B. D. and Weida, F. M., Statistics With Applications to Highway Traffic Analysis. Saugatuck: Eno Foundation for Highway Traffic Control, 1952.
- 7. Hejal, S. S. and Michael, H. L., "A Predictive Model for Travel Times on Two-Lane Highways." J.H.R.P. No. 19, (1970).
- 8. Helly, W. and Baker, P. G., "Acceleration Noise in a Congested Signalized Environment." Vehicular Traffic Science, (1967).
- 9. Highway Research Board, "Highway Capacity Manual." H.R.B. Special Report 87, (1965).
- 10. Institute of Traffic Engineers, Manual of Traffic Engineering Studies. Washington: Institute of Traffic Engineers, 1964.
- 11. Jones, T. R. and Potts, R. B., "The Measurement of Acceleration Noise A Traffic Parameter." Operations Research, X (1962), 745-763.



- 12. Lilliefors, H. W., "On the Kolmogorov-Smirnov Test for Normality with Mean and Variance Unknown."

 Journal of the American Statistical Association,

 LXII (June 1967), 400.
- 13. Matson, T. M., Smith, W. S., and Hurd, F. W., <u>Traffic</u> Engineering. New York: McGraw-Hill, 1955.
- 14. Miller, I. and Freund, J. E., <u>Probability and Statistics for Engineers</u>. Englewood Cliffs: Prentice-Hall, Inc., 1965.
- 15. Ostle, B., Statistics in Research. Ames: The Iowa State University Press, 1963.
- 16. Snedecor, G. W. and Cochran, W. G., Statistical Methods. Ames: The Iowa State University Press, 1967.
- 17. Statistical Laboratory Library Programs, Purdue University.
- 18. Votaw, D. F. and Levinson, H. S., <u>Elementary Sampling</u> for Traffic Engineers. Saugatuck: Eno Foundation for Highway Traffic Control, 1962.
- 19. Webster, L. A., "Traffic Delay on Urban Arterial Streets as a Result of Curb Parking Maneuvers." H.R.B. Record 267, (1967).
- 20. Wohl, M. and Martin, B. V., <u>Traffic System Analysis</u> for Engineers and Planners. New York: McGraw-Hill, 1967.



APPENDIX A DISCUSSION OF THE FOSTER-BURR Q-TEST



THE Q-TEST FOR EQUALITY OF VARIANCES*

by

Louis A. Foster and Irving W. Burr

The Q-test for equality of variances is based on a statistic which is a monotone function of the coefficient of variation of the sample variances.** As such it offers promise as a preliminary test for the assumption of homogeneity of population variances which is needed in the analysis of variance technique.*** Although the Q-test is not a so-called quick test, the test statistic is sufficiently simple to permit calculation of its value on a desk calculator (in contrast to the logarithmic transformation required in Bartlett's test). A sample variance taking the value zero does not disrupt this test (as it does to Bartlett's and Hartley's tests). Finally, a table of critical values permits the use of this test for small sample sizes where the use of an asymptotic distribution would not be appropriate.

THE Q-STATISTIC: For equal sample sizes, n, from each of p parent populations, let s? (for j = 1, ..., p) denote the jth sample variance. Denoting the value of the test statistic Q by q, we have:

$$q = (s_1^4 + ... + s_p^4)/(s_1^2 + ... + s_p^2)^2$$
.

For unequal sample sizes we specify that each sample variance, s_j^2 , be calculated by dividing by the degrees of freedom, v_j , rather than by the sample size, n_j (where

^{*}This brief summary of the Q-test is based on a Ph.D. thesis submitted to Purque University by Louis A. Foster working under the supervision of Irving W. Burr.

^{**}Equivalent tests have been proposed by Brandt and Stevens, but in a form depending solely on an asymptotic distribution for the test statistics.

^{***}This statement is based on the role of the coefficient of variation of the population variances in measuring the disruption of the F-ratio in the analysis of variance technique, as set forth by Box (6) Vol. 25, pages 290 and 484.



 $v_j = n_j - 1$, for j = 1, ..., p). Let \bar{v} denote the arithmetic average of the degrees of freedom. In this case we have:

$$q = \overline{v} (v_1 s_1^4 + ... + v_p s_p^4) / (v_1 s_1^2 + ... + v_p s_p^2)^2$$

THE Q-TEST: Large values of Q lead to rejection of the hypothesis of equal population variances. The critical values are given in the attached table for various numbers of parent populations, p, and various possibilities for equal degrees of freedom, v (where v = n - 1), from one to ten. This table can be used directly for equal degrees of freedom. For unequal degrees of freedom, q is calculated as indicated above, but v is to be substituted for v in the attached table, provided that v and the harmonic mean of the v's do not differ greatly. For large sample sizes (v > 10), we note that p v (pQ-1)/2 is asymptotically chisquare with (p-1) degrees of freedom.



The 95th and 99th Percentiles of Q for Equal Degrees of Freedom and Equal Population Variances

(the upper entry in each cell is to be used for .05 level tests and the lower entry for .01 level tests).

	10	.751	.453	.341	.272	.226	.168	.149	.134	.111	.0823
	6	.681	.529	.350	.280	.233	.173	.153	.138	.114	.0845
	ω	.700	.479	.362	.290	.241	.179	.159	.142	.118	.0874
= n-1	7	.722	.497	.377	.302	.251	.187	.166	.148	.123	.0910
reedom (v		.750	.520	.396	.318	.264	.297	.175	.156	.129	.0958
s of F	Ŋ	.785	.548	.422	.339	.283	.211	.187	.168	.139	.103
The Degree	4	.829	.594	.485	.371	.310	.232	.206	.284	.153	.113
Ţ	m	. 988	.658	.517	.421	.353	.322	.236	.212	.176	.130
	7	.951	.747	.612	.510	.433	.331	.295	.330	.221	.164
	1	9999	.923	.814	.708	.662	.495	. 577	. 527	. 448	.339
		7	m	4	Ŋ	9	ω	9	10	12	16



10	.0479	.0402	.0197
6	.0492	.0413	.0202
œ	.0507	.0425	.0208
7	.0527	.0442	.0216
9	.0554	.0464	.0226
2	.0592	.0495	.0240
4	.0650	.0543	.0262
٣	.0747	.0623	.0299
7	.0944	.0787	.0375
1	.155	.129	.0613
	27	32	64

8			
		1	

APPENDIX B NORMALITY TEST FOR SECTION SPEEDS

	١

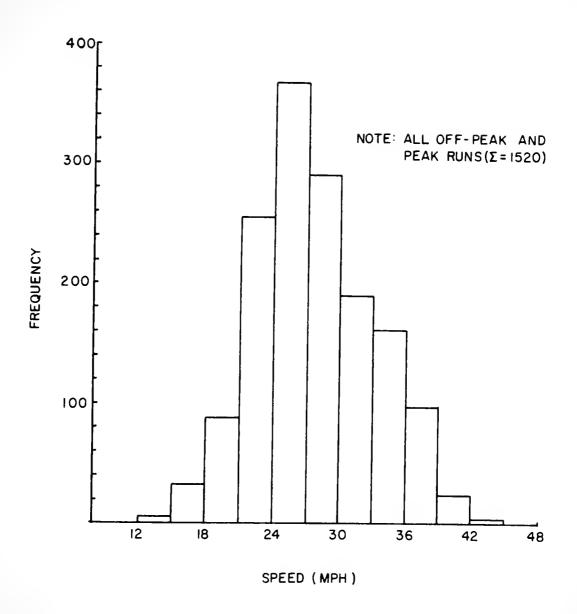


FIGURE BI. FREQUENCY OF SECTION SPEEDS



TABLE B1

NORMALITY TEST FOR SECTION SPEEDS (OFF-PEAK AND PEAK)

		(20)	Cumulative		Normal Curve Cumulative
Class	Frequency	Frequency	(8)	23	(8)
12.000-14.999	9	9	0.4	-2.39	0.842
15.000-17.999	32	38	2.5	-1.83	3.362
18.000-20.999	88	126	8.3	-1.26	10.383
21.000-23.999	255	381	25.1	-0.70	24.196
24.000-26.999	368	749	49.3	-0.14	44.433*
27.000-29.999	291	1040	68.4	+0.42	66.276
30.000-32.999	191	1231	81.0	+0.99	83.891
33.000-35.999	162	1393	91.6	+1.55	93.943
36.000-38.999	86	1491	98.1	+2.11	98.257
39.000-41.999	25	1516	7.66	+2.67	99.621
42.000-44.999	4	1520	100.0	+3.23	98.938

*Denoted Location of Maximum Deviation.

			,

Calculations for the Kolmogorov-Smirnov Test for the Normality of the Section Speeds

Critical D for 1520 samples (Level of Significance = 0.01)

$$D_{c} = \frac{1.031}{(N)^{1/2}}$$
 (12)

$$D_{c} = \frac{1.031}{(1520)} = 0.0264$$

Maximum Deviation = 0.0487

0.0487 > 0.0264

Therefore, reject hypothesis that the curve is normal.

APPENDIX C NORMALITY TEST FOR RESIDUALS

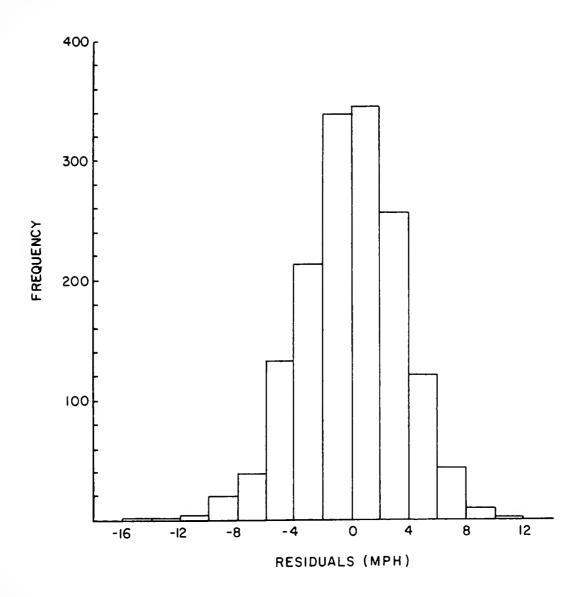


FIGURE CI. FREQUENCY OF RESIDUALS



TABLE C1

NORMALITY TEST FOR RESIDUALS

	Frequency	Cumulative Frequency	Cumulative Frequency (%)	N	Normal Curve Cumulative Frequency
	1	1	0.1	-4.10	1
	1	2	0.1	-3.52	0.022
	3	Ŋ	0.3	-2.93	0.169
	19	24	1.6	-2.34	0.964
	38	62	4.1	-1.76	3.920
	132	194	12.8	-1.17	12.100
	213	407	26.8	-0.59	27.760*
	339	746	49.1	0	50.000
	345	1091	71.8	65.0	72.240
	256	1347	88.5	1.17	87.900
	120	1467	5.96	1.76	080.96
	43	1510	99.3	2.34	98.036
	6	1519	6.66	2.93	99.831
	1	1520	100.0	3.52	99.978
*Denotes location	of maximum deviation.	iation.			



Claculations for the Kolmogorov-Smirnov Test for the Normality of the Residuals

Critical D for 1520 samples (Level of Significance = 0.05)

$$D_{C} = \frac{0.886}{(N)^{1/2}}$$
 (12)

$$D_{C} = \frac{0.886}{(1520)} = 0.0228$$

Maximum Deviation = 0.0096

0.0096 < 0.0228

Therefore, cannot reject hypothesis that the curve is normal.

-4	



